Modern Astronomy

Part 1. Interstellar Medium (ISM)

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- In general, equilibrium means a state of balance.
- Thermal Equilibrium
 - Thermal equilibrium refers to steady states of temperature, which defines the average energy of material or photons.

(for ideal gas,
$$E_{\text{avg}} = \frac{3}{2}k_{\text{B}}T$$
)

- In a state of (complete) *thermodynamic equilibrium (TE)*, no net flows of matter or of energy, no phase changes, and no unbalanced potentials (or driving forces), within the system. *In TE, matter and radiation are in equilibrium at the same temperature T.*
- When the material is (locally) in thermodynamic equilibrium, and only the radiation field is allowed to depart from its TE, we refer to the state of the system as being in *local thermodynamic equilibrium (LTE)*
- In other words, if the material is (locally) in thermodynamic equilibrium at a welldefined temperature *T*, *it is said to be in local thermodynamic equilibrium (LTE) even if it is not in equilibrium with the radiation field.*

Blackbody

- Imagine a container bounded by opaque walls with a very small hole.
 - Photons will be scattered and absorbed many times, (and eventually trapped and completely absorbed in the box). Under such conditions, the particles and photons continually share their kinetic energies. In perfect thermal equilibrium, the average particle kinetic energy will equal to the average photon energy, and a unique temperature T can be defined.
 - A blackbody is an idealized physical body that absorbs all incident radiation regardless of frequency or angle of incidence (i.e., perfect absorber). The above cavity can be regarded to be a blackbody.
 - Radiation from a blackbody in thermal equilibrium is called the blackbody radiation.



box 1

Blackbody radiation is the universal function.

- Now, consider another cavity (box 2), also at the same temperature, but made of different material or shape and connect two cavities with a filter transparent only in the narrow frequency range ν and $\nu + d\nu$.
 - In equilibrium at T, radiation should transfer no net energy from one cavity to the other. Otherwise, one cavity will cool down and the other heats up; this violates the second law of thermodynamics.
 - Therefore, the intensity or spectrum that passes through the holes should be a universal function of *T* and should be isotropic.
 - The intensity and spectrum of the radiation emerging from the hole should be independent of the wall material (e.g., wood, copper, or concrete, etc) and any absorbing material that may be inside the cavity.
 - The universal function is called the Planck function $B_{\nu}(T)$.
 - This is the blackbody radiation.



In (full) thermodynamic equilibrium at temperature T, by definition, we know that

$$\frac{dI_{\nu}}{ds} = 0$$
 and $I_{\nu} = B_{\nu}(T)$

We also note that

$$\frac{dI_{\nu}}{ds} = -\alpha_{\nu}I_{\nu} + j_{\nu}$$

- Then, we can obtain *the Kirchhoff's law for a system in TE*:

$$\frac{j_{\nu}}{\alpha_{\nu}} = B_{\nu}(T), \qquad j_{\nu} = \alpha_{\nu}B_{\nu}(T)$$

- Kirchhoff's law applies not only in TE but also in LTE:
 - Recall that $B_{\nu}(T)$ is independent of the properties of the radiating /absorbing material.
 - In contrast, both $j_{\nu}(T)$ and $\kappa_{\nu}(T)$ depend only on the materials in the cavity and on the temperature of that material; they do not depend on the ambient radiation field or its spectrum.
 - Therefore, the Kirchhoff's law should be true even for the case of LTE.
 - In LTE, the ratio of the emission coefficient to the absorption coefficient is a function of temperature and frequency only.

Blackbody radiation vs. Thermal radiation

- Blackbody radiation means $I_{\nu} = B_{\nu}(T)$. An object for which the intensity is the Planck function is emitting blackbody radiation.
- Thermal radiation is defined to be radiation emitted by "matter" in LTE. Thermal radiation means $S_{\nu} = B_{\nu}(T)$. An object for which the source function is the Planck function is emitting thermal radiation.
- Thermal radiation becomes blackbody radiation only for optically thick media.

- To see the difference between thermal and blackbody radiation,
 - Consider a slab of material with optical depth τ_{ν} that is producing thermal radiation.
 - If no light is falling on the back side of the slab, the intensity that is measured on the front side of the slab is

$$I_{\nu}(\tau_{\nu}) = I_{\nu}(0)e^{-\tau_{\nu}} + S_{\nu}\left(1 - e^{-\tau_{\nu}}\right)$$
$$I_{\nu}(0) = 0 \\ S_{\nu} = B_{\nu} \longrightarrow \qquad = B_{\nu}\left(1 - e^{-\tau_{\nu}}\right)$$

- If the slab is optical thick at frequency ν ($\tau_{\nu} \gg 1$), then

$$I_{\nu} = B_{\nu} \quad \text{as } \tau_{\nu} \to \infty$$

- If the slab is optically thin $(\tau_{\nu} \ll 1)$, then

$$I_{\nu} \approx \tau_{\nu} B_{\nu} \ll B_{\nu} \quad \text{as } \tau_{\nu} \ll 1$$

This indicates that the radiation, although it is thermal, will not be blackbody radiation.

Thermal radiation becomes blackbody radiation only for optical thick media.



Spectrum of Blackbody Radiation

- In reality, there is no perfect blackbody.
 - However, the cosmic microwave background comes quite close; stars can sometimes be usefully approximated as blackbodies.
 - By the end of the 19th century, the blackbody spectrum was fairly well known empirically, from laboratory studies. In 1900, Max Planck, using his idea of quantized energies, derived the blackbody spectrum.



https://pages.uoregon.edu/imamura/321/122/lecture-3/stellar_spectra.html

The frequency dependence of blackbody radiation is given by the *Planck function*:

$$B_{\nu}(T) = \frac{2h\nu^{3}/c^{2}}{\exp(h\nu/k_{\rm B}T) - 1} \text{ or } B_{\lambda}(T) = \frac{2hc^{2}/\lambda^{5}}{\exp(hc/\lambda k_{\rm B}T) - 1}$$

 $h = 6.63 \times 10^{-27}$ erg s (Planck's constant) $k_{\rm B} = 1.38 \times 10^{-16}$ erg K⁻¹ (Boltzmann's constant)

Stefan-Boltzmann Law

- Emergent flux is proportional to T^4 .

Stephan – Boltzmann constant : $\sigma = \frac{2\pi^5 k_{\rm B}^4}{15c^2h^3} = 5.67 \times 10^{-5} \text{ erg cm}^2 \text{ s}^{-1} \text{ K}^{-4} \text{ sr}^{-1}$

Blackbody Radiation: Properties. Rayleign-Jeans Law & Wien Law

Rayleigh-Jeans Law (low-energy limit)



Wien Law (high-energy limit)

 $h\nu \gg k_{\rm B}T$

$$I_{\nu}^{W}(T) = \frac{2h\nu^{3}}{c^{2}} \exp\left(-\frac{h\nu}{k_{\rm B}T}\right)$$



• Brightness Temperature:

- The brightness temperature is defined to be the temperature such that a blackbody at that temperature would have specific intensity:

$$I_{\nu} = B_{\nu}(T_b) \rightarrow T_b(\nu) = \frac{h\nu/k_{\rm B}}{\ln\left[1 + 2h\nu^3/(c^2 I_{\nu})\right]}$$

Antenna Temperature:

- Radio astronomers are used to working at very low frequencies. They define the antenna temperature as being the brightness temperature in the Rayleigh-Jeans tail.

$$I_{\nu} = \frac{2\nu^2}{c^2} k_{\rm B} T_b \quad \rightarrow \quad T_A \equiv \frac{c^2}{2k_{\rm B}\nu^2} I_{\nu}$$

- Radiative transfer equation in the RJ limit:
 - If the matter is in LTE and has its energy levels populated according to an excitation temperature $T_{\rm exc} \gg h\nu/k_{\rm B}$, then the source function is given by

 $S_{\nu}(T_{\rm exc}) = (2\nu^2/c^2)k_{\rm B}T_{\rm exc}$

Then, RT equation becomes

$$\frac{dT_A}{d\tau_{\nu}} = -T_A + T_{\text{exc}} \quad \text{if } h\nu \ll k_{\text{B}}T_{\text{exc}} \qquad \frac{dI_{\nu}}{d\tau_{\nu}} = -I_{\nu} + S_{\nu}$$

$$T_A = T_A(0)e^{-\tau_{\nu}} + T_{\text{exc}}(1 - e^{-\tau_{\nu}})$$
 if T_{exc} is constant.

Color Temperature:

- By fitting the spectrum to a blackbody curve without regarding to vertical scale (absolute intensity scale), a color temperature T_c is obtained.
- The color temperature correctly gives the temperature of a blackbody source of unknown absolute scale.
- Effective Temperature:
 - The effective temperature of a source is obtained by equating the actual flux F to the flux of a blackbody at temperature $T_{\rm eff}$.

$$F = \int \int I_{\nu} \cos \theta d\nu d\Omega = \sigma T_{\rm eff}^4$$
 cf. Stefan-Boltzmann law

- Excitation Temperature:
 - The excitation temperature of level u relative to level ℓ is defined by

cf. Boltzmann distribution

$$\frac{n_u}{n_\ell} = \frac{g_u}{g_\ell} \exp\left(-\frac{E_{u\ell}}{k_B T_{exc}}\right) \quad \to \quad T_{exc} \equiv \frac{E_{u\ell}/k_B}{\ln\left(\frac{n_\ell/g_\ell}{n_u/g_u}\right)} \quad (E_{u\ell} \equiv E_u - E_\ell)$$

- Radio astronomers studying the 21 cm line sometimes use the term "spin temperature" for excitation temperature.

Brief Introduction to Atomic Spectroscopy

[Reference]

Astronomical Spectroscopy:

An Introduction to the Atomic and Molecular Physics of Astronomical Spectra author: Jonathan Tennyson, 2nd Edition

- Each bound state of the hydrogen atom is characterized by a set of four quantum numbers (n, l, m, m_s)
 - $n = 1, 2, 3, \cdots$: principal quantum number (shell)
 - $l = 0, 1, 2, \dots, n-1$: *orbital angular momentum* quantum number (subshell)
 - By convention, the values of l are usually designated by small letters.

0	1	2	3	4	5	6	7	8	
S	р	d	f	g	h	i	k	1	• • •

- $m = -l, -l + 1, \dots, 0, \dots, l 1, l$: magnetic quantum number.
 - It determines the behavior of the energy levels in the presence of a magnetic field.
 - This is the projection of the electron orbital angular momentum along the z-axis of the system.
- Spin
 - _ The electron possesses an intrinsic, **spin angular momentum** with the magnitude of $|s| = \frac{1}{2}$.

_ There are two states,
$$m_s = \pm \frac{1}{2}$$
, for the spin.

• Degeneracy for a given *n*: $2 \times \sum_{l=0}^{n-1} (2l+1) = 2n^2$

- Spectral series of the H atom
 - The spectrum of H is divided into a number of series linking different upper levels n₂ with a single lower level n₁ value. *Each series is denoted according to its* n₁ *value and is named after its discoverer.*
 - Within a given series, individual transitions are labelled by Greek letters.

$n_2 \longleftrightarrow n_1$								
n_1	Name	Symbol	Spectral region					
1 2 3 4 5	Lyman Balmer Paschen Brackett Pfund	Ly H P Br Pf	ultraviolet visible infrared infrared infrared					
6	Humphreys	Hu	infrared					

$\Delta n \equiv n_2 - n_1$	Lyman series : $Ly\alpha$, $Ly\beta$, $Ly\gamma$,
$\Delta n = 1$ is α , $\Delta n = 2$ is β	Balmer series : $H\alpha$, $H\beta$, $H\gamma$, Paschen series: $P\alpha$, $P\beta$, $P\gamma$, Brackett series : $Br\alpha$, $Br\beta$, Brw ,
$\Delta n = 2$ is ρ , $\Delta n = 3$ is γ ,	Transitions with high Λn are labelled by
$\Delta n = 4$ is δ ,	the n_2 . Thus, $H15$ is the Balmer series
$\Delta n = 5$ is ϵ .	transition between $n_1 = 2$ and $n_2 = 15$.

Schematic energy levels of the hydrogen atom with various spectral series identified. The vertical numbers are wavelengths in Å.



Complex Atoms : Electron Configuration

- The configuration is the distribution of electrons of an atom in atomic orbitals.
 - The configuration of an atomic system is defined by specifying the nl values of all the electron orbitals: nl^x means x electrons in the orbital defined by n and l.
 - Each orbital labelled nl actually consists of orbitals with 2l + 1 different m values, each with two possible values of m_s . Thus the nl orbital can hold a maximum 2(2l + 1) electrons.

 $1s^2 2s^2 2p^6 3s^2 3p^6 3d^{10} \cdots$

<u>shells</u>, <u>subshells</u>:

- Principal quantum number = shell: Shells correspond with the principal quantum numbers (1, 2, 3, ...). They are labeled alphabetically with letters used in the X-ray notation (K, L, M, ...).
- Orbital angular momentum quantum number = subshell: Each shell is composed of one or more subshells. The first (K) shell has one subshell, called "1s"; The second (L) shell has two subshells, called "2s" and "2p".

Angular Momentum Coupling

- Atoms contain several sources of angular momentum.
 - electron orbital angular momentum L
 - *electron spin* angular momentum S
 - nuclear spin angular momentum I
 - The nuclear spin arises from the spins of nucleons. Protons and neutrons both have an intrinsic spin of a half.
- As in classical mechanics, only the total angular momentum is a conserved quantity.
 - It is therefore necessary to combine angular momenta together.
- Addition of two angular momenta:
 - The orbital and spin angular momenta are added vectorially as J = L + S. This gives the total electron angular momentum.
 - One then combines the total electron and nuclear spin angular momenta to give the final angular momentum $\mathbf{F} = \mathbf{J} + \mathbf{I}$.

¹⁹ Lifting Degeneracy in Configuration: Angular Momentum Coupling, Terms

L-S coupling (Russell-Saunders coupling):

- The orbital and spin angular momenta are added separately to give the total orbital angular momentum L and the total spin angular momentum S. These are then added to give J.

$$L = \sum_{i} l_{i}, S = \sum_{i} s_{i} \rightarrow J = L + S$$

- The configurations split into terms with particular values of L and S.
- Adding two Angular Momenta
 - Adding vector a and vector b gives a vector c, whose length lies in the range

$$|a-b| \le c \le a+b$$
 Here, a, b, c are the lengths of their respective vectors.
 $c = |a-b|$ $c = a+b$

In quantum mechanics, a similar rule applies except that the results are quantized. The allowed values of the quantized angular momentum, *c*, span the range from the sum to the difference of *a* and *b* in steps of one:

$$c = |a - b|, |a - b| + 1, \dots, a + b - 1, a + b$$

- For example, add the two angular momenta $L_1 = 2$ and $L_2 = 3$ together to give $L = L_1 + L_2$. The result is

$$L = 1, 2, 3, 4, 5.$$

- Electronic configuration and energy level splitting
 - Configurations ⇒ Terms ⇒ Fine Structure (Spin-Orbit Interaction) ⇒ Hyperfine Structure (Interaction with Nuclear Spin)



[Pradhan & Nahar] Atomic Astrophysics and Spectroscopy

The Fine Structure of Hydrogen

- So far the discussion on H-atom levels has assumed that all states with the same principal quantum number, n, have the same energy.
 - However, this is not correct: inclusion of relativistic (or magnetic) effects split these levels according to the total angular momentum quantum number *J*. *The splitting is called fine structure.*

• For hydrogen,
$$S = \frac{1}{2} \rightarrow J = L \pm \frac{1}{2}$$

Spectroscopic notation:

$$(2S+1)L_{I}$$

configuration	L	S	J	term	level
ns	0	1/2	1/2	^{2}S	${}^{2}S_{1/2}$
np	1	1/2	$1/2, \ 3/2$	$^{2}P^{o}$	${}^{2}P_{1/2}^{o}, \; {}^{2}P_{3/2}^{o}$
nd	2	1/2	3/2, 5/2	^{2}D	${}^{2}D_{3/2}, \; {}^{2}D_{5/2}$
nf	3	1/2	5/2, 7/2	${}^{2}F^{o}$	${}^2F^o_{5/2}, \; {}^2F^o_{7/2}$

Note that the levels are called to be						
singlet if $2S+1 = 1$	$S = 0, \ J = L$					
doublet if $2S+1 = 2$	$S = 1/2, J = L \pm 1/2$					
triplet if $2S+1 = 3$	S = 1, J = L - 1, L, L + 1					
(when $L > 0$)						

- The above table shows the fine structure levels of the H atom.
- Note that the states with principal quantum number n = 2 give rise to three fine-structure levels. In spectroscopic notation, these levels are $2^2S_{1/2}$, $2^2P_{1/2}^o$ and $2^2P_{3/2}^o$.

Spectroscopic Notation

Spectroscopic Notation



sharp, principal, diffuse, fundamental,...

-

• J = L - 1, L, L + 1 (triplet $L \ge 1$)

Selection Rules



Allowed = Electric Dipole : Transitions which satisfy all the above selection rules are referred to as allowed transitions. These transitions are strong and have a typical lifetime of $\sim 10^{-8}$ s. Allowed transitions are denoted without square brackets.

e.g., C IV 1548, 1550 Å

Photons do not change spin, so transitions usually occur between terms with the same spin state $(\Delta S = 0)$. However, relativistic effects mix spin states, particularly for high *Z* atoms and ions. As a result, one can get (weak) spin changing transitions. These are called *intercombination (semi-forbidden or intersystem) transitions* or lines. They have **a typical lifetime of** $\sim 10^{-3}$ **s**. An intercombination transition is denoted with a single right bracket.

C III]
$$2s^{2} {}^{1}S - 2s2p {}^{3}P^{o}$$
 at 1908.7 Å. ($\Delta S = 1$)

If any one of the rules 1-4, 6-8 are violated, they are called *forbidden transitions* or lines. They have **a typical lifetime of** $\sim 1 - 10^3$ **s**. A forbidden transition is denoted with two square brackets.

1906.7 Å [C III] $2s^{2-1}S_0 - 2s2p^{-3}P_2^o$, ($\Delta S = 1, \Delta J = 2$)

Resonance line denotes a dipole-allowed transition arising from the ground state of a particular atom or ion.

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- Forbidden lines are often difficult to study in the laboratory as collision-free conditions are needed to observe metastable states.
 - In this context, it must be remembered that laboratory ultrahigh vacuums are significantly denser than so-called dense interstellar molecular clouds.
 - Even in the best vacuum on Earth, frequent collisions knock the electrons out of these orbits (metastable states) before they have a chance to emit the forbidden lines.
 - In astrophysics, low density environments are common. In these environments, the time between collisions is very long and an atom in an excited state has enough time to radiate even when it is metastable.
 - Forbidden lines of nitrogen ([N II] at 654.8 and 658.4 nm), sulfur ([S II] at 671.6 and 673.1 nm), and oxygen ([O II] at 372.7 nm, and [O III] at 495.9 and 500.7 nm) are commonly observed in astrophysical plasmas.
 - The forbidden 21-cm hydrogen line is particularly important for radio astronomy as it allows very cold neutral hydrogen gas to be seen.
 - Since metastable states are rather common, forbidden transitions account for a significant percentage of the photons emitted by the ultra-low density gas in Universe.
 - Forbidden lines can account for up to 90% of the total visual brightness of objects such as emission nebulae.

- Notations for Spectral Emission Lines and for Ions
 - There is a considerable confusion about the difference between these two ways of referring to a spectrum or ion, for example, C III or C⁺². These have very definite different physical meanings. However, in many cases, they are used interchangeably.
 - C⁺² is a baryon and C III is a set of photons.
 - C+2 refers to carbon with two electrons removed, so that is doubly ionized, with a net charge of +2.
 - C III is the spectrum produced by carbon with two electrons removed. The C III spectrum will be produced by impact excitation of C⁺² or by recombination of C⁺³. So, depending on how the spectrum is formed. C III may be emitted by C⁺² or C⁺³.

collisional excitation: $C^{+2} + e^- \rightarrow C^{+2*} + e^- \rightarrow C^{+2} + e^- + h\nu$ recombination: $C^{+3} + e^- \rightarrow C^{+2} + h\nu$

- There is no ambiguity in absorption line studies only C⁺² can produce a C III absorption line. This had caused many people to think that C III refers to the matter rather than the spectrum.
- But this notation is ambiguous in the case of emission lines.

Hydrogen Atom : Fine & Hyperfine Structures

Hyperfine Structure in the H atom

- Coupling the nuclear spin I to the total electron angular momentum J gives the final angular momentum F. For hydrogen this means

$$F = J + I = J \pm \frac{1}{2}$$



[Kwok] Physics and Chemistry of the ISM, [Bernath] Spectra of atoms and Molecules

• 3 electrons (Lithium-like ions)



[Draine] Physics of the Interstellar and Intergalactic Medium

• 5 & 8 electrons

Upward heavy: allowed, Upward Dashed: intercombination, Downward solid: forbidden



[Draine] Physics of the Interstellar and Intergalactic Medium

Multiphase ISM

Five Phases of the ISM

Molecular clouds

- H₂ is the dominant form of molecules.
- Number density ~ 10⁶ cm⁻³ in the molecular cloud cores, which are self-gravitating and form stars. (Note that 10⁶ cm⁻³ is comparable to the density in the most effective cryo-pumped vacuum chambers in laboratories.)
- How to observe: for instance, 2.6, 1.3 and 0.9 mm (115, 230 and 345 GHz) emission lines from CO.

Cold neutral medium (CNM) ($T \sim 10^2$ K)

- The dominant form of CNM is H I (atomic hydrogen).
- The CNM is distributed in sheets and filaments occupying ~1% of the ISM volume.
- How to observe: UV and optical absorption lines in the spectra of background stars and quasars.

Warm neutral medium (WNM) ($T \sim 5 \times 10^3$ K)

- Its dominant form is H I (atomic hydrogen).
- A leading method of observing the WNM is using 21 cm emission.

Warm ionized medium (WIM) or Diffuse ionized gas (DIG) ($T \sim 10^4$ K)

- The dominant form is H II (ionized hydrogen or proton).
- The WIM is primarily photoionized by O- and B- type stars.
- Observed using Balmer emission lines (H α).

Hot ionized medium (HIM) or coronal gas ($T \gtrsim 10^{5.5}$ K)

- The HIM is primarily heated by supernovae.
- HIM occupies \sim half of the ISM volume, but provides only 0.2% of the ISM mass.
- soft X-ray emission. O VI, N V, and C IV emission or absorption lines in the spectra of background stars.

Name	T (K)	$n_{\rm H}({\rm cm}^{-3})$	Mass fraction	Volume fraction
Molecular Clouds	20	>100	35%	0.1%
Cold Neutral Medium	100	30	35%	1%
Warm Neutral Medium	5000	0.6	25%	40%
Warm Ionized Medium	10^{4}	0.3	3%	10%
Hot Ionized Medium	10 ⁶	0.004	0.2%	50%





M51 (NGC5195) Plate 1 [Lequeux]

B band - blue V band - green Ha - red (DIG)



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- All five phases of the ISM have a pressure $P \sim 4 \times 10^{-19}$ atm, equivalent to a thermal energy density $(3/2)nkT \sim 0.4$ eV cm⁻³.
 - Thus, it is tempting to assume that the phases are in pressure equilibrium, with

 $n_1kT_1 = n_2kT_2 = 4 \times 10^{-19}$ atm $n_1T_1 = n_2T_2 = 2,935$ cm⁻³ K (1 atm = 1.013 × 10⁶ dyn cm⁻²)



- Earlier views of the ISM did assume the pressure equilibrium. Denser, cooler "clouds" in a tenuous, hotter "intercloud medium."
- However, current studies of the ISM have had reject this simple picture. The ISM has indeed tendencies toward pressure equilibrium, but something always happens to throw things out of equilibrium.
 - The ubiquity of free electrons indicates that the ISM is coupled to the interstellar magnetic field. The turbulent energy density is not negligibly small. Thus, they have to be taken into account.
 - ✦ Supernova explosions are going off in the ISM, increasing the temperature T.
 - Hot young stars are pouring ionizing radiation into the ISM, splitting up atoms and increasing n.

- The temperature of the ISM is also determined by a balance between heating and cooling.
 - Each phase has a temperature where the balance is a stable one.
- Definitions
 - Heating gain per atom G, Cooling loss per atom L in units of erg s⁻¹.
 - Volumetric heating rate g = nG, Volumetric cooling rate $\ell = nL$ in units of erg cm⁻³ s⁻¹.
 - Cooling function Λ in units of erg cm³ s⁻¹, which is useful for *two-body interactions*.
 - $\ell = nL = n^2 \Lambda$, where *n* is the total number density of gas particles.
 - Even when only one type of particle is losing energy, the energy loss is shared among all the gas particles due to the relatively short thermalization time scale in the ISM.

Reference: Collisional time scale in the CNM

- $t_{coll}(HH) \sim 2.2 \, yr$ for atom-atom collisions
 - $t_{\rm coll}(e{\rm H}) \sim 120\,{
 m yr}$ for atom-electron collisions
- $t_{coll}(ee) \sim 1.2 \, hr$ for electron-electron collision

Mean free path in the CNM

- $\lambda_{\rm mfp}({\rm HH}) \sim 0.74 \,{\rm AU}$
- $\lambda_{\rm mfp}(e{\rm H}) \sim 1700 \,{\rm AU}$

for atom-atom collisions

- for atom-electron collisions
- , $\lambda_{\rm mfp}(ee) \sim 1.9 \times 10^{-3} \, {\rm AU}$ for electron-electron collision

Heating & Cooling in Neutral Medium

Heating processes

- The primary heating mechanisms of the ISM involve providing free electrons with high energies. Through collisions, the fast free electrons share their kinetic energy with other particles, and through further collisions, the distribution of velocities approaches a Maxwellian distribution.

- Source of free electrons

- Ionization by cosmic rays
- Photoionization of dust grains by starlight UV the most important one.
- Photoionization of atoms (H, He, C, Mg, Si, Fe, etc) by X-rays or starlight UV.

- Other heating sources:

- Heating by shock waves and other MHD phenomena.
- Cooling processes
 - Collisional excited lines ([C II], [O I], Ly α , etc)
 - Thermal bremsstrahlung

- Heating: Photoelectric Heating by Dust -

- UV and X-ray photons can knock electrons free from dust grains. The ejected electrons carry kinetic energy, which can be effective at heating the surrounding gas.
- Photoelectrons emitted by dust grains dominate the heating of the diffuse neutral ISM (CNM and WNM) in the Milky Way.
- The work function, analogous to the ionization energy of an atom, for graphite is $4.50 \pm 0.05 \,\text{eV}$. Therefore, UV photons with $h\nu \gtrsim 5 \,\text{eV}$ can kick out photoelectrons from dust grains. The photoelectric heating by dust is dominated by photons with $h\nu \gtrsim 8 \,\text{eV}$.

$$G_{\rm pe} \approx 1.4 \times 10^{-26} \frac{n_{\rm ph}(8 - 13.6 \,\mathrm{eV})}{3 \times 10^{-3} \,\mathrm{cm}^{-3}} \frac{\langle \sigma_{\rm abs} \rangle}{10^{-21} \,\mathrm{cm}^2} \frac{\langle Y \rangle}{0.1} \frac{\langle E_{\rm pe} \rangle - \langle E_c \rangle}{1 \,\mathrm{eV}} \quad \mathrm{erg \ s^{-1}}$$

The gain is independent of temperature.

Here,

 $\begin{array}{l} n_{\rm ph}(8-13.6\,{\rm eV}) = {\rm number \ density \ of \ 8} < h\nu < 13.6\,{\rm eV} \ {\rm photons} \\ \left< \sigma_{\rm abs} \right> = {\rm total \ dust \ photo \ absorption \ cross \ section \ per \ H \ nucleon, \ averaged \ over \ the \ photon \ spectrum.} \\ \left< Y \right> = {\rm photoelectric \ yield \ averaged \ over \ the \ spectrum \ of \ 8 \ to \ 13.6 \ eV \ photons \ absorbed \ by \ the \ interstellar \ grain \ mixture.} \\ \left< E_{\rm pe} \right> = {\rm mean \ kinetic \ energy \ of \ electrons \ captured \ from \ the \ plasma \ by \ grains.} \end{array}$

- Photoelectric heating from dust may be an order of magnitude larger than the cosmic ray heating rate.

- Decreasing the average kinetic energy of particles in the ISM is usually done by *radiative cooling*.
 - In the CNM, cooling is performed by infrared photons emitted by carbon and oxygen.
 - Oxygen is nearly all in the form of neutral O I. (the ionization energy = 13.26 eV)
 - Carbon will be nearly always in the form of singly ionized C II. (ionization energy = 11.26 eV) The background starlight in our galaxy has enough photons in the relevant energy range $11.26 \text{ eV} < h\nu < 13.60 \text{ eV}$ to keep the C atoms ionized.
- [C II] 158µm (collisionally excited line emission)
 - The electronic ground state of C II is split into two fine levels, separated by an energy $E_{u\ell} = 7.86 \times 10^{-3} \,\text{eV}$, which corresponds to $\lambda = 158 \,\mu\text{m}$ and $T = E_{u\ell}/k = 91.2 \,\text{K}$.
 - The upper level is populated by collisions with hydrogen atoms and free electrons.
 - If C II is excited by collisions with free electrons, the cooling function is given by, for a C abundance $n_{\rm C}/n_{\rm H} = 3 \times 10^{-4}$,

$$\frac{\Lambda_{\text{[CII]}}^{e}}{10^{-25} \,\text{erg cm}^3 \,\text{s}^{-1}} \approx 0.03 \left(\frac{x}{10^{-3}}\right) \left(\frac{T}{100 \,\text{K}}\right)^{-1/2} \exp\left(-\frac{91.2 \,\text{K}}{T}\right)$$

Here, $x = n_e/n$ is the ionization fraction.

- If the CII is excited by collisions with hydrogen atoms, the cooling function is

$$\frac{\Lambda_{\rm [CII]}^{\rm H}}{10^{-25}\,{\rm erg}\,\,{\rm cm}^3\,\,{\rm s}^{-1}} \approx 0.06 \left(\frac{T}{100\,{\rm K}}\right)^{0.13} \exp\left(-\frac{91.2\,{\rm K}}{T}\right)$$

- In the CNM, both contribute significantly to the excitation of C II.



C II 158 µm line emission in the Galaxy. The map size is -180° to 180° in Galactic longitude and -60° and 60° in Galactic latitude. The data is from all-sky maps created by the Cosmic Microwave Background Explorer.

[Fig. 5.5. Introduction to the Interstellar Medium, J. P. Williams]

- [O I] 63.2µm (collisionally excited emission line)
 - The electronic ground state of O I has a fine splitting of $E_{u\ell}/k = 228$ K.
 - The upper level is populated primarily by collisions with hydrogen atoms.
 - The resulting cooling function due to the emission of 63.2µm is, for an abundance of $n_{\rm O}/n_{\rm H} = 5.4 \times 10^{-4}$,

$$\frac{\Lambda_{\rm [OI]}^{\rm H}}{10^{-25}\,{\rm erg}\,\,{\rm cm}^3\,\,{\rm s}^{-1}} \approx 0.04 \left(\frac{T}{100\,{\rm K}}\right)^{0.42} \exp\left(-\frac{228\,{\rm K}}{T}\right)$$

- Note:
 - [C II] and [O I] are the dominant form of cooling in molecular clouds and the CNM.
 - Molecular clouds can also cool by emission from the vibrational and rotational transitions of molecules.

Lyα 1216Å

- The first excited level of atomic hydrogen is $E_{21} = 10.20 \,\text{eV}$ above the ground state.
- Although the first excited level will not be highly populated by collisions until the temperature reaches $T \sim E_{21}/k = 118,000$ K, hydrogen is extremely abundant. Thus the cooling by Ly α can compete with cooling by IR fine-structure lines at temperature as low as T ~ 8000 K.
- The cooling function for H excited by collisions with free electrons is

$$\frac{\Lambda_{[Ly\alpha]}^{e}}{10^{-25} \,\mathrm{erg} \,\mathrm{cm}^{3} \,\mathrm{s}^{-1}} \approx 7000 \left(\frac{x}{10^{-3}}\right) \left(\frac{T}{100 \,\mathrm{K}}\right)^{-0.5} \exp\left(-\frac{118,000 \,\mathrm{K}}{T}\right)$$





- For $10 < T < 10^3$ K, [C II] 158µm line is a major coolant. The [O I] 63µm line is important for T > 100 K. Ly α cooling dominates only at T > 10⁴ K.

- Stable & Unstable

- A thermal equilibrium must have heating
 - We assume *photoelectric heating by dust* and the equilibrium density is obtained by



- If every point along the above equilibrium line represented a stable equilibrium, then there could be a continuous distribution of temperatures, and thus of number densities.
- However, it's not the case. Not every equilibrium point is a stable equilibrium.

- Pressure Equilibrium -

Let's assume that the interstellar gas is in pressure equilibrium.

- For pressures in the range $0.7 \times 10^{-13} \text{ dyn cm}^{-2} < P < 7 \times 10^{-13} \text{ dyn cm}^{-2}$, bounded by the dashed lines, there are three possible values of n_{eq} at a fixed pressure.
- Consider what happens at a point, for instance F, if you slightly change the temperature while keeping the pressure fixed.
- If T increases, n must decrease, and you must move left from point F. This moves you into the net cooling portion, and T consequently decreases.
- If T decrease, n must increase, and this moves you rightward into the net heating portion, and T consequently increases.
- Thus, a negative feedback restores the original temperature.
- A similar negative feedback maintains temperature stability at point H.
- However, now consider what happens at G.
- If T increases, n must decrease, and you must move left from point G. This moves you into the net heating portion, and T increases further, until you reach F.
- If T decrease, n must increase, and this moves you rightward into the net cooling portion, and T decrease further, until you reach H.
- Thus, a positive feedback makes the point unstable.
- Consequently, we have two stable equilibrium points (F and H). F = WNM, H = CNM



Two-Phase Model & Three-Phase Model

- As a result of their analysis, Field, Goldsmith, and Habing (1969) created a two-phase model of the ISM, consisting of Cold Neutral Clouds, with n ~ 10 cm⁻³ and T ~ 100 K, embedded within a Warm Intercloud Medium, with n ~ 0.1 cm⁻³ and T ~ 10,000 K.
 - They were unaware of the role played by dust in heating the ISM, assumed that collisional ionization by cosmic rays provided the bulk of the heating.
 - FGH (1969) advocated a two-phase model. However, they also speculated "an existence of a third stable phase at T > 10⁶ K, with bremsstrahlung the chief cooling process."
- In the 1970s, detection of a diffuse soft X-ray background and of emission lines such as O VI 1032, 1038Å hinted at the existence of interstellar gas with T ~ 10⁶ K. In fact, the Sun resides in a "Local Bubble" of hot gas, with T ~ 10⁶ K and n ~ 0.004 cm⁻³.
- Cox & Smith (1974) suggested that supernova remnants could produce a bubbly hot phase, and that the bubbles blown by supernovae would occupy a large volume fraction of the ISM.
- A superbubble or supershell is a cavity which is ~100 pc across and is populated with hot (10⁶ K) gas atoms, less dense than the surrounding ISM, blown against that medium and carved out by multiple supernovae and stellar winds.



McKee & Ostriker's Three-Phase Model

- McKee & Ostriker (1977)
 - They made a more elaborate argument for three phases within the ISM.
 - Cold Neutral Medium, with $T \sim 80$ K, $n \sim 40$ cm⁻³, and a low fractional ionization $x = n_e/n \lesssim 0.001$.
 - *Warm Medium*, containing both ionized and neutral components, $T \sim 8000$ K and $n \sim 0.3$ cm⁻³, the ionization fraction ranging from $x \sim 0.02$ in the neutral component (WNM) to $x \sim 0.15$ in the ionized component (WIM).
 - *Hot Ionized Medium*, consisting of the overlapping supernova bubbles, with $T \sim 10^6$ K and $n \sim 0.002$ cm⁻³, and $x \sim 1$ (nearly complete ionization).



 However, in many ways, the ISM is a dynamic, turbulent, dusty, magnetized place.

Homework (due date: 09/20)

[Q1] Consider an (isotropically emitting) star of uniform intensity $I_{\nu} = B$ at the surface, show that the flux at the surface is

$$F_{\nu} = \int I_{\nu} \cos \theta d\Omega = \pi B$$

[reference] Radiative Processes in Astrophysics (Rybicki & Lightman)

[Q2] (a) The specific intensity of a star is, to first order, a blackbody. For a given effective temperature, $T_{\rm eff}$, and stellar radius, R, derive its bolometric luminosity.

(b) Look up values for these parameters and calculate this formula for the Sun.